

<name>

Class: Honors Geometry

Date: <date>

Topic: Lesson 7-7 (Areas of Circles and Sectors)

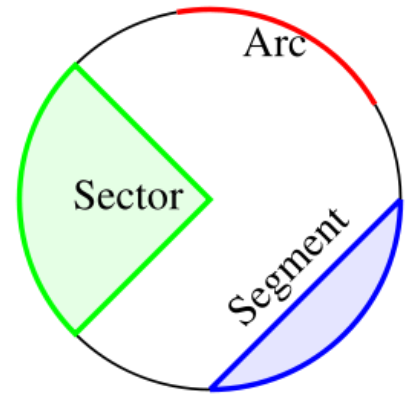
Theorem 7-15 | Area of a Circle

$$A = \pi r^2$$

Definition

Sector

Region of circle btwn two radii & the included arc.



Theorem 7-16 | Area of a Sector of a Circle

$$\text{The area of sector } AOB = \frac{m\widehat{AB}}{360} \cdot \pi r^2$$

Example

Find the area of sector ACB . Leave your answer in terms of π .

$$m\widehat{AB} = 100; \text{ area } \odot C = \pi(6)^2 = 36\pi$$

$$\text{Area of sector } AOB = \frac{m\widehat{AB}}{360} \cdot \pi r^2 = \frac{100}{360} \cdot 36\pi = \frac{100}{10} \cdot \pi = 10\pi \text{ m}^2$$

Definition

Segment of a Circle

The part of a sector btwn the arc & a segment joining its endpts.

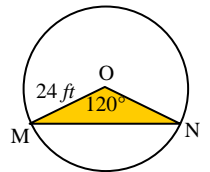
Formula

Area of a segment

Area of segment = area of sector – area of triangle.

Example

Find the area of the segment MON . Round your answer to the nearest tenth.



$$\text{Area of sector: } \frac{m\widehat{MN}}{360} \cdot \pi r^2 = \frac{120}{360} \cdot \pi 24^2 = \frac{1}{3} \cdot \pi \cdot 24 \cdot 24 = 8 \cdot 24 \cdot \pi = 192\pi$$

Area of triangle: 30-60-90 w/h = short leg & long leg $\frac{1}{2}$ the base:

$$h = 24 \div 2 = 12; \quad b = 2 \cdot 12\sqrt{3} = 24\sqrt{3}; \quad A = \frac{1}{2}bh = \frac{1}{2} \cdot 12 \cdot 24\sqrt{3} = 144\sqrt{3}$$

$$\text{Area of segment: } 192\pi - 144\sqrt{3} \approx 353.77 \approx 353.8 \text{ ft}^2$$

